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06MAT31

**Third Semester B.E. Degree Examination, Dec.09/Jan.10
Engineering Mathematics - III**

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART - A

- 1 a. Obtain Fourier series for the function $f(x)$ given by

$$f(x) = \begin{cases} 1 + \frac{2x}{\pi}, & -\pi \leq x \leq 0 \\ 1 - \frac{2x}{\pi}, & 0 \leq x \leq \pi \end{cases}$$

and hence deduce that $\frac{\pi^2}{8} = \frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots$ (07 Marks)

- b. Find the half-range cosine series for the function $f(x) = (x-1)^2$ in the interval $0 < x < 1$. (07 Marks)
- c. Obtain the constant term and the coefficients of the first sine and cosine terms in the Fourier expansion of y as given in the following table. (06 Marks)

x	0	1	2	3	4	5	6
y	9	18	24	28	26	20	9

- 2 a. Find the Fourier transform of $f(x) = \begin{cases} 1-x^2, & |x| \leq 1 \\ 0, & |x| > 1 \end{cases}$

Hence evaluate $\int_0^{\infty} \frac{x \cos x - \sin x}{x^3} \cdot \cos\left(\frac{x}{2}\right) dx$ (07 Marks)

- b. Find the Fourier cosine transform of e^{-x^2} (07 Marks)
- c. Find the Fourier sine transform of $e^{-|x|}$. Hence show that $\int_0^{\infty} \frac{x \sin mx}{1+x^2} dx = \frac{\pi}{2} e^{-m}$, $m > 0$. (06 Marks)

- 3 a. Form the partial differential equation by eliminating the arbitrary functions f and g from the relation $z = y^2 + 2f\left(\frac{1}{x} + \log y\right)$ (07 Marks)

b. Solve $\frac{\partial^3 t}{\partial x^2 \partial y} + 18xy^2 + \sin(2x - y) = 0$ (07 Marks)

c. Solve $(mz - ny) \frac{\partial z}{\partial x} + (nx - lz) \frac{\partial z}{\partial y} = (ly - mx)$ (06 Marks)

- 4 a. Derive one dimensional heat equation by taking $u(x, t)$ as the temperature, x is the distance and t is the time. (Write the figure also.) (07 Marks)

b. Obtain the D'Alembert's solution of the wave equation $u_{tt} = C^2 u_{xx}$, subject to the condition $u(x, 0) = f(x)$ and $\frac{\partial u}{\partial t}(x, 0) = 0$. (07 Marks)

c. Obtain the various solutions of the Laplace's equation $u_{xx} + u_{yy} = 0$, by the method of separation of variables. (06 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and/or equations written eg, 42+8 = 50, will be treated as malpractice.

PART – B

- 5 a. Complete the real root of the equation $x \log_{10} x - 1.2 = 0$ by Regula-Falsi method, correct to four decimal places. (07 Marks)
- b. Solve the system of equations using Gauss-Jordan method:
 $2x + 5y + 7z = 52$
 $2x + y - z = 0$
 $x + y + z = 9$ (07 Marks)
- c. Using the power method, find the largest Eigen value and the corresponding Eigen vector of the matrix $A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$ (06 Marks)
- 6 a. The area of a circle (A) corresponding to diameter (D) is given below: (07 Marks)
- | | | | | | |
|---|------|------|------|------|------|
| D | 80 | 85 | 90 | 95 | 100 |
| A | 5026 | 5674 | 6362 | 7088 | 7854 |
- Find the area corresponding to diameter 105 using an appropriate interpolation formula.
- b. Use Newton's divided difference formula to find $f(9)$, given the data, (07 Marks)
- | | | | | | |
|------|-----|-----|------|------|------|
| x | 5 | 7 | 11 | 13 | 17 |
| f(x) | 150 | 392 | 1452 | 2366 | 5202 |
- c. Evaluate $\int_4^{5.2} \log_e x \, dx$ using Weddle's rule, taking 7 ordinates. (06 Marks)
- 7 a. Derive Euler's equation in the form
 $\frac{\partial f}{\partial y} - \frac{d}{dx} \left(\frac{\partial f}{\partial y'} \right) = 0$ (07 Marks)
- b. Find the curves on which the functional $\int_0^1 [(y')^2 + 12xy] dx$, with $y(0) = 0$ and $y(1) = 1$ can be extremised. (07 Marks)
- c. Find the geodesics on a surface given that the arc length on the surface is
 $S = \int_{x_1}^{x_2} \sqrt{x[1 + (y')^2]} dx$ (06 Marks)
- 8 a. Find the Z-transforms of the following :
 i) $\cosh n\theta$ ii) $(n + 1)^2$ (07 Marks)
- b. Find the inverse z-transform of $\frac{z}{(z-1)(z-2)}$. (07 Marks)
- c. Find the response of the system $y_{n+2} - 5y_{n+1} + 6y_n = u_n$, with $y_0 = 0$, $y_1 = 1$ and $u_n = 1$ for $n = 0, 1, 2, 3, \dots$ by z-transform method. (06 Marks)

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Third Semester B.E. Degree Examination, Dec.09/Jan.10
Analog Electronic Circuits

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART - A

- 1 a. Describe how diffusion and transition capacitances differ. (05 Marks)
- b. A full wave bridge rectifier is supplied from the transformer secondary voltage of 100 V. Calculate the dc output voltage and peak inverse voltage of the diodes employed. (05 Marks)
- c. For the clipper circuit shown in the Fig.1(c), the input is $V_i = 50 \sin \omega t$. Calculate and plot to scale the transfer characteristic, indicating slopes and intercepts. (10 Marks)

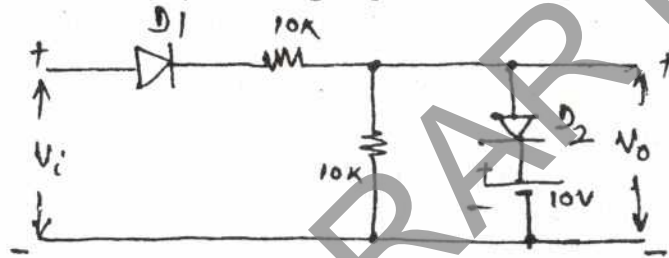


Fig.1(c).

- 2 a. Determine the voltage V_{CE} and I_C for the voltage divider configuration shown in Fig.2(a). (10 Marks)

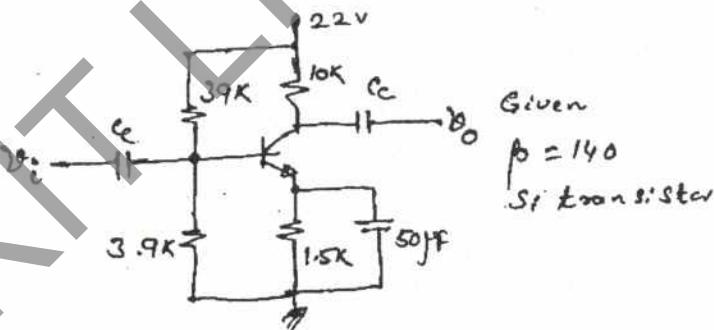


Fig.2(a).

- b. Determine R_1 and R_c for the network of Fig.2(b). Given $I_{CQ} = 2 \text{ mA}$, $V_{CEQ} = 10 \text{ V}$. Assume S_i transistor. (10 Marks)

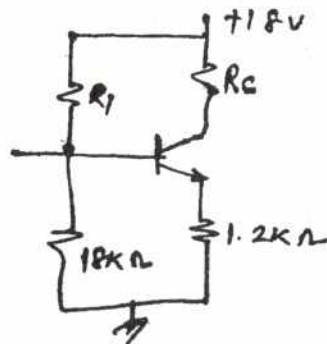
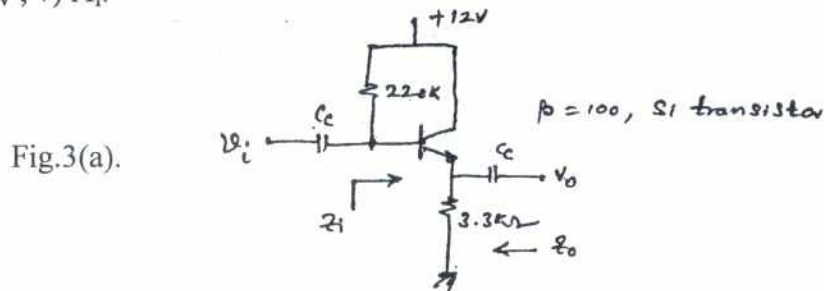


Fig. 2(b)

Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
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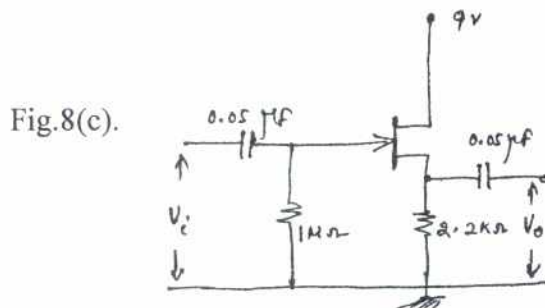
- 3 a. For the emitter – follower network of Fig.3(a), using r_e model determine: i) r_e ; ii) z_i ; iii) z_o ; iv) A_V ; v) A_I . (10 Marks)



- b. Using complete hybrid equivalent model for a two part system derive expressions for A_i , A_V , z_i and z_o . (10 Marks)
- 4 a. Prove that Miller effect capacitance $C_{Mi} = (1 - A_V) c_f$ and $C_{Mo} = (1 - 1/A_V) c_f$. (10 Marks)
- b. A four stage amplifier has a lower 3 db frequency for an individual stage of $f_1 = 40$ Hz and individual upper 3 db frequency of $f_2 = 2.5$ MHz. Calculate the overall lower 3 db and upper 3 db frequency of this full amplifier. Derive the expressions used. (10 Marks)

PART – B

- 5 a. Explain with the help of circuits what is cascade connection and cascode connection. What are the advantages of these connections? (10 Marks)
- b. Explain the important advantages of a negative feedback amplifier. (04 Marks)
- c. List the four types of feedback connections. Show one practical circuit for each feedback connection. (06 Marks)
- 6 a. Explain the working of a transformer coupled class B push pull amplifier. (10 Marks)
- b. A Class B amplifier provides a 20 V peak signal to a 16 ohm load and a power supply of $V_{cc} = 30$ V. Determine the input power, output power and circuit efficiency. (05 Marks)
- c. Calculate the harmonic distortion components for an output signal, having a fundamental amplitude of 2.5 V, second harmonic amplitude of 0.25 V, third harmonic amplitude of 0.1 V and fourth harmonic amplitude of 0.05 V. Also calculate the total harmonic distortion. (05 Marks)
- 7 a. Explain Barkhausen criterion for oscillations. (05 Marks)
- b. With the help of a neat circuit diagram, explain the working of Hartley oscillator. (07 Marks)
- c. List the advantages of a crystal oscillator. Explain the working of a series resonant crystal oscillator. (08 Marks)
- 8 a. List three advantages of JFET over BJT. (03 Marks)
- b. With a neat circuit diagram, explain potential divider biasing of JFET. (07 Marks)
- c. Calculate the voltage gain and input and output impedance for the circuit of Fig.8(c). (10 Marks)



Given:

$$I_{DSS} = 16 \text{ mA}$$

$$V_p = -4 \text{ V}$$

$$r_d = 40 \text{ K } \Omega$$

$$V_{GSQ} = -2.86 \text{ V.}$$

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Third Semester B.E. Degree Examination, Dec.09/Jan.10
Logic Design

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART – A

- 1 a. Show that $y = f(ABCD) = \sum(0, 2, 5, 7, 8, 10, 13, 15)$ is the complement of $y = f(ABCD) = \pi(1, 3, 4, 6, 9, 11, 12, 14)$. Illustrate your answer using Karnaugh map to show the complement nature of the two equations. Realize both the functions using 7486 IC chip [Exclusive OR gates] only. (12 Marks)
- b. Design a logic circuit that controls the passage of a signal 'A' according to the following requirement.
- Output 'X' will equal 'A' when control inputs B and C are the same.
 - 'X' will remain 'HIGH' when B and C are different
- Implement the circuit using suitable gates. (08 Marks)
- 2 a. Simplify the following expression using Quine-McClusky technique. Implement the simplified circuit using basic gates: $f(ABCD) = \sum(1, 3, 4, 5, 6, 9, 11, 12, 13, 14)$. (12 Marks)
- b. Simplify the following Boolean expression using VEM technique. [3 variable map].
 $f(ABCD) = \sum m(0, 4, 5, 6, 13, 14, 15) + dc(2, 7, 8, 9)$

A	B	C	D	f	A	B	C	D	f
0	0	0	0	1	1	0	0	0	ϕ
0	0	0	1	0	1	0	0	1	ϕ
0	0	1	0	ϕ	1	0	1	0	0
0	0	1	1	0	1	0	1	1	0
0	1	0	0	1	1	1	0	0	0
0	1	0	1	1	1	1	0	1	1
0	1	1	0	1	1	1	1	0	1
0	1	1	1	ϕ	1	1	1	1	1

 ϕ = don't care term.

(08 Marks)

- 3 a. Design a logic circuit using a 3 to 8 logic decoder that has active low data inputs, an active HIGH enable and active low data outputs. Use such a decoder to realize the full adder circuit. (08 Marks)
- b. Design a suitable BCD adder circuit using 74LS83 and a provision has to be made for self correction in case if the sum is not a valid BCD number format. (12 Marks)
- 4 a. Implement the following Boolean function using 4 :1 MUX
 $y(ABCD) = \sum m(0, 1, 2, 4, 6, 9, 12, 14)$. (10 Marks)
- b. Design a circuit that accepts 2 unsigned 4 bit numbers and provides 3 outputs. The inputs are $A_3 A_2 A_1 A_0$ and $B_3 B_2 B_1 B_0$. Outputs are $A = B$, $A > B$ and $A < B$. Draw the logic diagram. (10 Marks)

PART - B

- 5 a. Explain the following:
- Switch debouncing and its elimination
 - Race around problem and its elimination.
- (14 Marks)
- b. Obtain the characteristic equation for the following flip flops:
- JK flip flop
 - SR flip flop.
- (06 Marks)
- 6 a. With the help of a diagram, explain the following with respect to shift register:
- Parallel in and serial out
 - Ring counter and twisted ring counter.
- (08 Marks)
- b. Design a Mod - 5 synchronous counter using JK flip flop.
- (12 Marks)
- 7 a. With a suitable example, explain Mealy and Moore model in a sequential circuit analysis.
- (10 Marks)
- b. A sequential circuit has one input and one output. The state diagram is as shown in Fig.7(b). Design a sequential circuit with 'T' flip flop.
- (10 Marks)

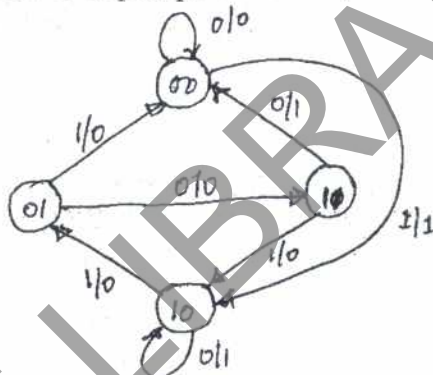


Fig.7(b).

- 8 a. Analyse the following sequential circuit shown in Fig.8(a) and obtain:
- Flip flop input and output equations.
 - Transition equation
 - Transition table
 - State table
 - Draw the state diagram.

(12 Marks)

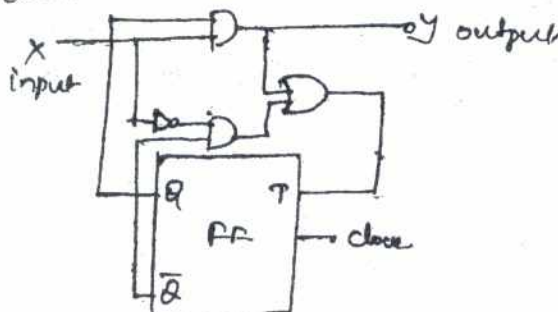


Fig.8(a).

- b. With a suitable example and appropriate state diagram, explain how to recognize a particular sequence. Ex: 1011. (Any sequence can be assumed).
- (08 Marks)

Third Semester B.E. Degree Examination, Dec.09/Jan.10 Network Analysis

Time: 3 hrs.

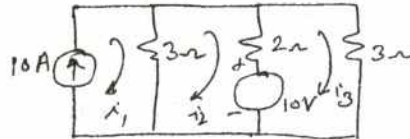
Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART - A

- 1 a. Write the mesh equations for the circuit shown in Fig.1 and solve for currents i_1 , i_2 and i_3 . (10 Marks)

Fig.1(a)



- b. The node voltage equations of a network are $\left(\frac{1}{5} + \frac{1}{2}j + \frac{1}{4}\right) v_1 - \frac{1}{4} v_2 = \frac{50 \angle 0^\circ}{5}$ and $-\frac{1}{4} v_1 + \left(\frac{1}{4} - \frac{1}{j2} + \frac{1}{2}\right) v_2 = \frac{50 \angle 90^\circ}{2}$. Derive the network. (10 Marks)

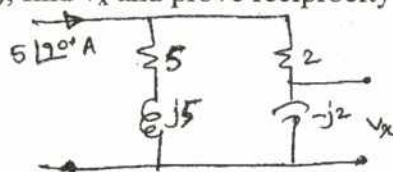
- 2 a. Define the following terms with respect to the network topology. Give examples.
i) Tree ; ii) Graph ; iii) Sub graph ; iv) Tieset ; v) Cutset. (08 Marks)
- b. For the network shown in Fig.2(b), write the graph and obtain the tieset schedule considering j_1, j_2, j_5 as tree branches. Also calculate all branch currents. (12 Marks)

Fig.2(b)



- 3 a. In the circuit shown in Fig.3(a), find v_x and prove reciprocity theorem. (10 Marks)

Fig.3(a)



- b. State and explain super position theorem with a suitable example. (10 Marks)

- 4 a. Obtain the Thevenin's equivalent network for the circuit in Fig.4(a) between the terminals X and Y. (10 Marks)

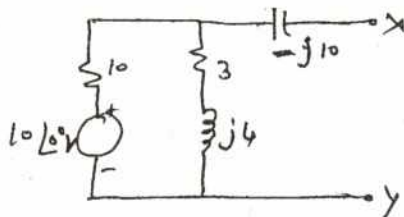


Fig.4(a).

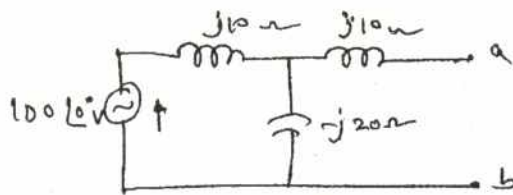
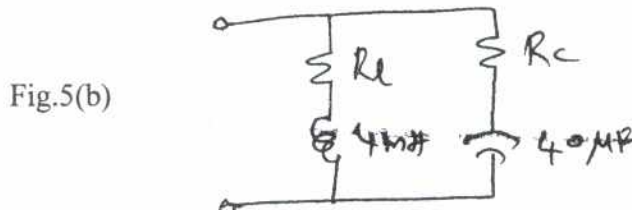


Fig.4(b).

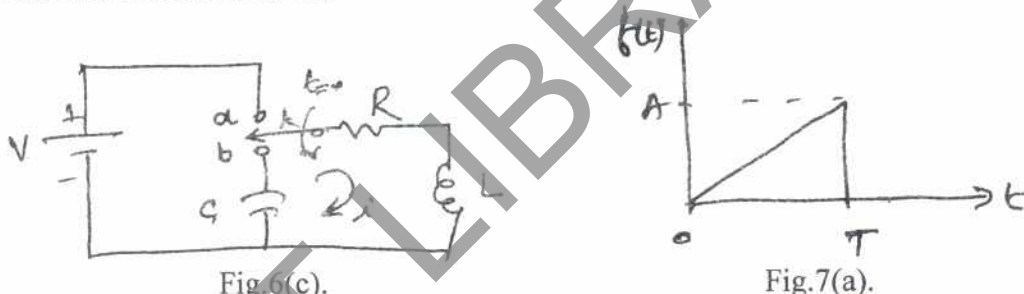
- b. What should be the value of pure resistive load to be connected across the terminals a and b in the network shown in Fig. 4(b), so that maximum power is transferred to the load? Calculate the maximum power. (10 Marks)

PART - B

- 5 a. Show that for a series RLC resonant circuit the selectivity $\phi = \frac{f_0}{f_2 - f_1}$, where f_0 : resonate frequency f_1 and f_2 are half power frequency. (08 Marks)
- b. Determine R_L and R_C for which the circuit shown in Fig.6 resonates at all frequencies. (06 Marks)



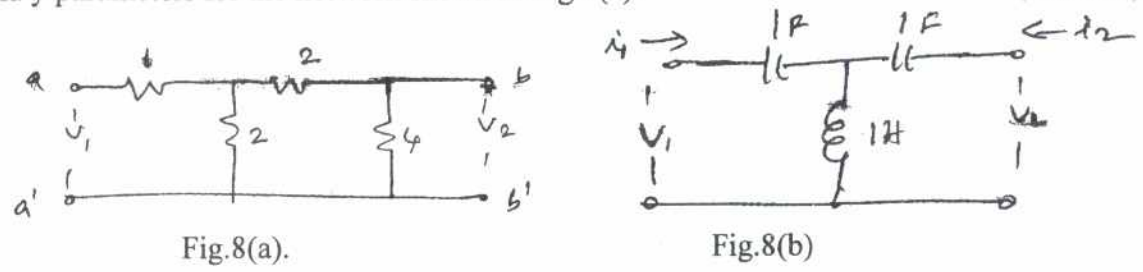
- c. It is required that a series RLC circuit should resonate at 1 MHz. Determine values of R, L and C if bandwidth of the circuit is 5 kHz and its impedance is 50 Ω at resonance. (06 Marks)
- 6 a. Explain the importance of study of initial conditions in electric circuit analysis. (06 Marks)
- b. Explain the behaviour of R, L and C elements for transients. Mention their representation at the instant of switching. (06 Marks)
- c. In the circuit shown in Fig.6(c), the switch is moved from 'a' to 'b' at $t = 0$. Find the values of i , $\frac{di}{dt}$, $\frac{d^2i}{dt^2}$ at $t = 0^+$, if $R = 1 \Omega$, $L = 1 H$, $C = 0.1 \mu F$ and $V = 100 V$. Assume steady state is achieved when k is at 'a'. (08 Marks)



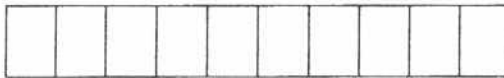
- 7 a. Obtain the Laplace transform of saw tooth waveform shown in Fig.7(a). (06 Marks)
- b. Find the Laplace transform of i) $\delta(t)$; ii) t ; iii) e^{-at} . (06 Marks)
- c. Find $f(0)$ and $f(\infty)$ using initial value and final value theorem for the function given below. (08 Marks)

$$F(s) = \frac{s^3 + 7s^2 + 5}{s(s^3 + 3s^2 + 4s + 2)}$$

- 8 a. Find y parameters for the network shown in Fig.8(a). (08 Marks)



- b. Determine the 'h' parameters for the network shown in Fig.8(b). (08 Marks)
- c. Mention the application of
 i) Transmission parameters ; ii) 'h' parameters ; iii) 'z' parameters. (04 Marks)



Third Semester B.E. Degree Examination, Dec.09/Jan.10
Electronic Instrumentation

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART – A

- 1 a. Explain the following:
 - i) Systematic errors
 - ii) Relative errors. (04 Marks)
- b. Explain the working principle of multi-range voltmeter, with the help of suitable circuit diagram. (08 Marks)
- c. Convert a basic meter movement with an internal resistance of 50Ω and a full scale deflection current of 2 mA in to a multi-range 'dc' voltmeter with voltage ranges of $0\text{-}10\text{V}$, $0\text{-}50\text{V}$, $0\text{-}100\text{V}$ and $0\text{-}250\text{V}$ with following Fig.1(c). (08 Marks)

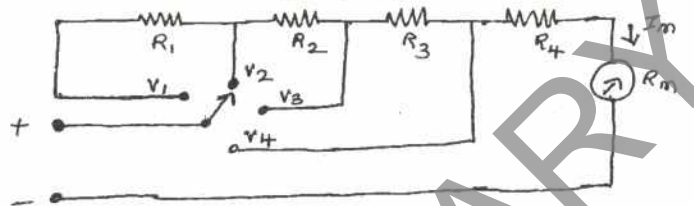


Fig.1(c).

- 2 a. Explain the ramp type digital voltmeter with the help of block diagram. (10 Marks)
- b. Explain the digital multimeter with basic circuit diagram. (10 Marks)
- 3 a. Explain the C.R.T. features briefly. (06 Marks)
- b. With the basic block diagram, explain the principle of operation of simple C.R.O. (08 Marks)
- c. Explain the operation of an electronic switch, with the help of a block diagram. (06 Marks)
- 4 a. Explain the principle and operation of sampling oscilloscope. What are its advantages and disadvantages? (10 Marks)
- b. Explain the operation of digital storage-oscilloscope with the help of a block diagram. Mention the advantages. (10 Marks)

PART – B

- 5 a. With a block diagram, explain modern laboratory signal generator. (10 Marks)
- b. Sketch the circuit and waveforms for an OP-AMP astable multivibrator for use as a square wave generator. Explain its operation. (10 Marks)
- 6 a. Explain the Wheatstone bridge and derive the balance equation for Wheatstone bridge. (06 Marks)
- b. Explain AC bridge and derive the balance equation for capacitance comparison bridge. (08 Marks)
- c. Find the equivalent parallel resistance and capacitance that causes a wein bridge to null with the following components values:
 $R_1 = 3.1 \text{ k}\Omega$, $c_1 = 5.2 \mu\text{F}$, $R_2 = 25 \text{ k}\Omega$, $f = 2.5 \text{ kHz}$ and $R_4 = 100 \text{ k}\Omega$ (06 Marks)
- 7 a. Explain the potentiometer with figure. (06 Marks)
- b. Explain the resistance thermometer with circuit diagram. (06 Marks)
- c. Explain the construction, principle and operation of LVDT. Show characteristics curve. (08 Marks)
- 8 a. Explain piezo electrical transducer, with circuit diagram. (06 Marks)
- b. Explain the light emitting diodes (LED) with diagram. (06 Marks)
- c. Explain how power is measured using a bolometer, with a suitable diagram. (08 Marks)

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Third Semester B.E. Degree Examination, Dec.09/Jan.10
Field Theory

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART – A

- 1 a. Define electric field intensity due to a point charge in vector form. With usual notations, derive the expression for field at a point due to many charges. (07 Marks)
- b. State and prove divergence theorem. (05 Marks)
- c. Calculate the divergence of vector D at the points specified using cartesian, cylindrical and spherical coordinates:
- i) $D = \frac{1}{z^2} [10xyz \cdot a_x + 5x^2za_y + (2z^3 - 5x^2y)a_z]$ c/m² at point P(2, 3, 5)
- ii) $D = 5z^2 \cdot a_\rho + 10\rho z \cdot a_z$ at $\rho(3, -45^\circ, 5)$ (08 Marks)
- 2 a. Define electric field and electric potential. With usual notations establish the relationship between electric field intensity and electric potential. (10 Marks)
- b. With usual notations, derive the boundary conditions for perfect dielectric materials of permittivities ϵ_1 and ϵ_2 . (05 Marks)
- c. Given the potential field $V = 50x^2yz + 20y^2$ volts in free space, find
- i) Potential V at P(1, 2, 3)
- ii) $|E_p|$ (Magnitude of electric potential)
- iii) \hat{a}_r at P. (05 Marks)
- 3 a. With usual notations, deduce the Poisson's equation and Laplace equation from Maxwell's first equation. Express ∇^2V in different co-ordinate systems. (10 Marks)
- b. Given $V = A \ln \left[B \frac{(1 - \cos\theta)}{1 + \cos\theta} \right]$ volts
- i) Show that V satisfies Laplace equation in spherical coordinates.
- ii) Find A and B so that $V = 100V$, $|E| = 500$ V/m at $r = 5$ mt, $\theta = 90^\circ$ and $\phi = 60^\circ$. (10 Marks)
- 4 a. State and prove the Stroke's theorem. (06 Marks)
- b. If the vector magnetic potential at a point in a space is given as $A = 100 \rho^{1.5} a_z$ wb/mt, find the following: i) H ii) J and show that $\oint H \cdot dI = I$ for the circular path with $\rho = 1$. (06 Marks)
- c. In cylindrical coordinates, a magnetic field is given as $H = [4\rho - 2\rho^2] a_\phi$ A/m, $0 \leq \rho \leq 1$.
- i) Find the current density or a function of ρ within cylinder.
- ii) Find the total current that passes through the surface $Z = 0$ and $0 \leq \rho \leq 1$ mt in the a_z direction. (08 Marks)

PART – B

- 5 a. With usual notations, derive the equation for magnetic force between two differential current elements. (06 Marks)
- b. Find the torque vector on a square loop having corners $(-2, -2, 0)$, $(2, -2, 0)$, $(2, 2, 0)$ and $(-2, 2, 0)$ i) about the origin by $B = 0.4a_x T$ ii) About the origin by $B = 0.6a_x - 0.4a_y T$. (06 Marks)
- c. Determine the mutual inductance between conducting loop and a very long straight wire shown in Fig.5(c). (08 Marks)

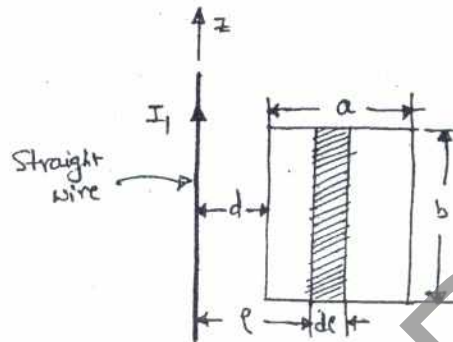
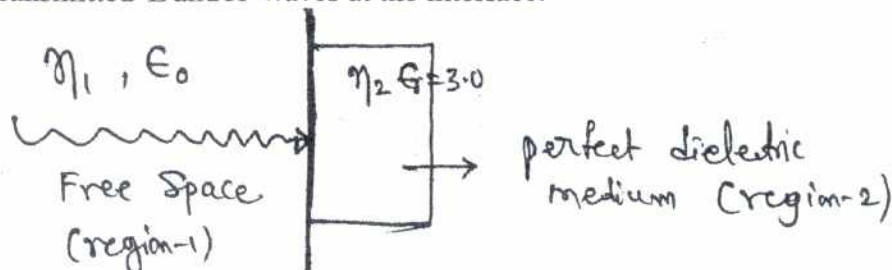


Fig.5(c)

- 6 a. With usual notations, derive the Maxwell's equation in point form as derived from Faraday's law. Hence show that electric field $E = 2x^3 a_x + 4x^4 a_y$ v/m can not arise from a static distribution of charges. (08 Marks)
- b. With usual notations, derive the differential form of continuity equation from the Maxwell's equations. (04 Marks)
- c. The time varying magnetic field in free space is given as $B = \begin{cases} 4 \sin \omega t a_z & \rho \leq \rho_0 \\ 0 & \rho > 0 \end{cases}$
Determine E using Faraday's law. Verify the same using Maxwell's equations. (08 Marks)
- 7 a. State and explain Poynting theorem. (04 Marks)
- b. With usual notations, derive the expression for intrinsic impedance for lossy media. (06 Marks)
- c. The electric field intensity of 300 MHz uniform plane wave in free space is given by $E = (20 + j50)(a_x + 2a_y)e^{-\beta z}$ V/m. Find
i) ω , λ , u and β ii) E at $t = 1$ ns $z = 10$ cm iii) What is $|H|_{\max}$? (10 Marks)
- 8 a. Write a short note on standing wave ratio (SWR). (04 Marks)
- b. With usual notations, derive a general expression for a traveling plane wave. (06 Marks)
- c. Travelling \vec{E} and \vec{H} waves in the free space (region-1) are normally incident on the interface with a perfect dielectric (region-2) with $\epsilon_r = 3.0$. Compare the magnitude of the incident wave and transmitted \vec{E} and \vec{H} waves at the interface.



(10 Marks)

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Third Semester BE Degree Examination, Dec.09-Jan.10
Advanced Mathematics – I

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions.

- 1 a. Find the modulus and amplitude of $\frac{4+2i}{2-3i}$. (06 Marks)
- b. Express the complex number $2+3i+\frac{1}{1-i}$ in the form of $a+ib$. (07 Marks)
- c. Express the complex number $\sqrt{3}+i$ in the polar form. (07 Marks)
- 2 a. Find the n^{th} derivative of $e^{-x} \sin^2 x$. (06 Marks)
- b. Find the n^{th} derivative of $\frac{x}{(x-1)(2x+3)} + e^{2x}$. (07 Marks)
- c. If $y = \sin^{-1} x$ then prove that $(1+x^2)y_{n+2} - (2n+1)xy_{n+1} - n^2y_n = 0$. (07 Marks)
- 3 a. Using Maclaurin's series expand $\tan x$ upto the term containing x^3 . (06 Marks)
- b. Find the angle between the radius vector and tangent to the curve $r = \sin\theta + \cos\theta$. (07 Marks)
- c. With usual notations prove that
- i) $P = r \sin\phi$
- ii) $\frac{1}{p^2} = \frac{1}{r^2} + \frac{1}{p^4} \left(\frac{dr}{d\theta} \right)^2$. (07 Marks)
- 4 a. If $u = f(r, s, t)$ where $r = \frac{x}{y}$, $s = \frac{y}{z}$, $t = \frac{z}{x}$ then prove that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z} = 0$. (06 Marks)
- b. If $u = f(x+ay) + g(x-ay)$ then show that $\frac{\partial^2 u}{\partial y^2} = a^2 \frac{\partial^2 u}{\partial x^2}$. (07 Marks)
- c. If $u = x^2 - 2y$, $v = x + y + z$, $w = x - 2y + 3z$ then find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$. (07 Marks)
- 5 a. Obtain the reduction formula for $\int \cos^n x dx$ where n is a positive integer. (06 Marks)
- b. Evaluate $\int_0^1 x^6 \sqrt{1-x^2} dx$. (07 Marks)
- c. Evaluate $\int_0^1 \int_x^{\sqrt{x}} (x^2 + y^2) dy dx$. (07 Marks)

Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and/or equations written eg. 42+8=50, will be treated as malpractice.

- 6 a. Evaluate $\int_0^1 \int_0^2 \int_0^2 x^2 yz \, dz dy dx$. (06 Marks)
- b. Prove that $\sqrt{\frac{1}{2}} = \sqrt{\pi}$. (07 Marks)
- c. Show that $\int_0^{\pi/2} \sqrt{\sin \theta} \, d\theta \times \int_0^{\pi/2} \frac{d\theta}{\sqrt{\sin \theta}} = \pi$. (07 Marks)
- 7 a. Solve $(e^y + 1) \cos x dx + e^y \sin x dy = 0$. (06 Marks)
- b. Solve $y dx - x dy = \sqrt{x^2 + y^2} dx$. (07 Marks)
- c. Solve $x \frac{dy}{dx} + y = x^3 y^6$. (07 Marks)
- 8 a. Solve $4 \frac{d^3 y}{dx^3} + 4 \frac{d^2 y}{dx^2} + \frac{dy}{dx} = 0$. (06 Marks)
- b. Solve $\frac{d^2 x}{dt^2} + 2 \frac{dx}{dt} + 3x = \sin t + e^{-t}$. (07 Marks)
- c. Solve $\frac{d^2 y}{dx^2} - 2 \frac{dy}{dx} + y = x e^x \sin x$. (07 Marks)

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